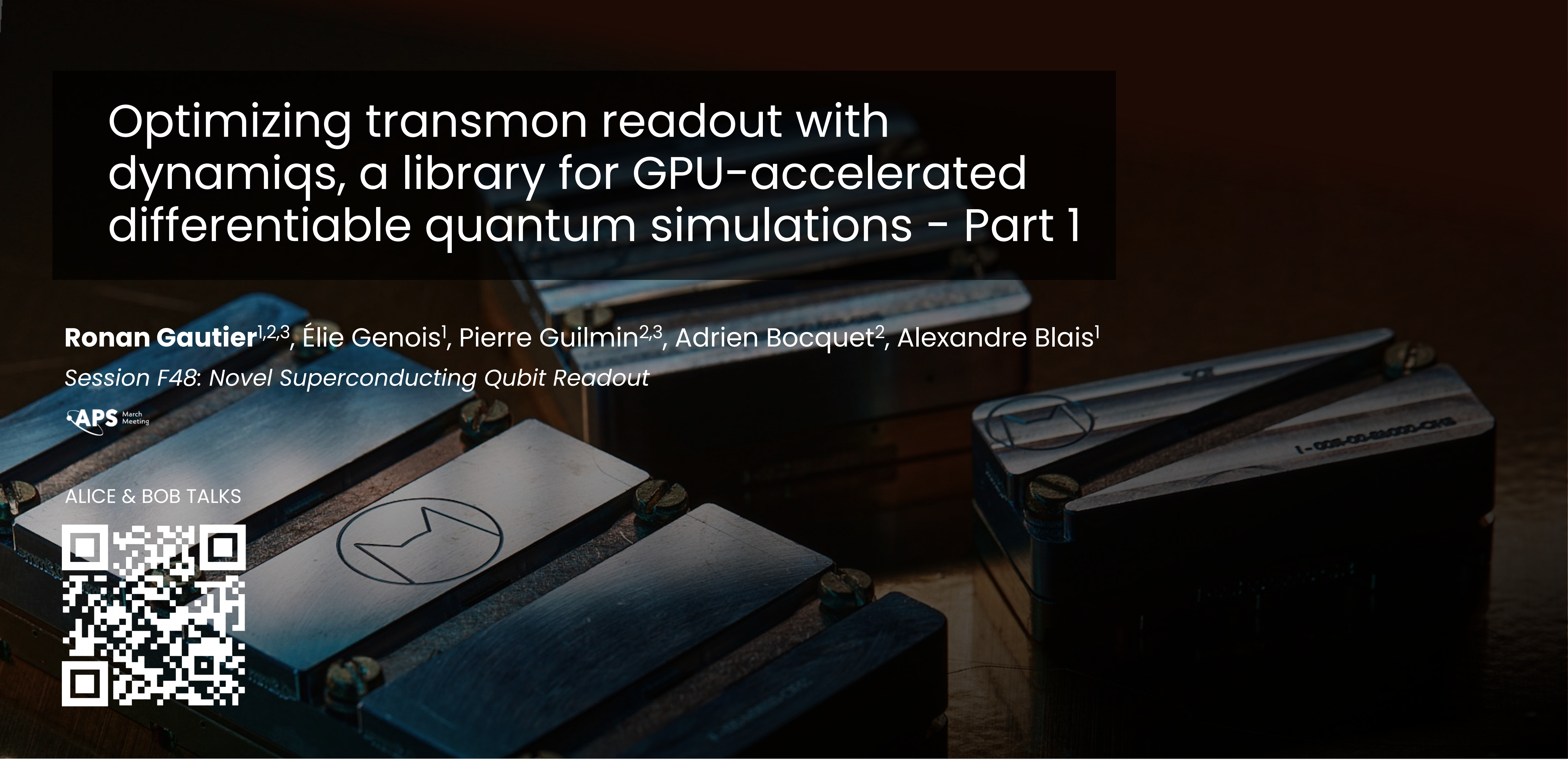
Optimizing transmon readout with dynamiqs, a library for GPU-accelerated differentiable quantum simulations - Part 1

Ronan Gautier[1,2,3], Élie Genois[1], Pierre Guilmin[2,3], Adrien Bocquet[2], Alexandre Blais[1]

Session F48: Novel Superconducting Qubit Readout

APS March Meeting

ALICE & BOB TALKS



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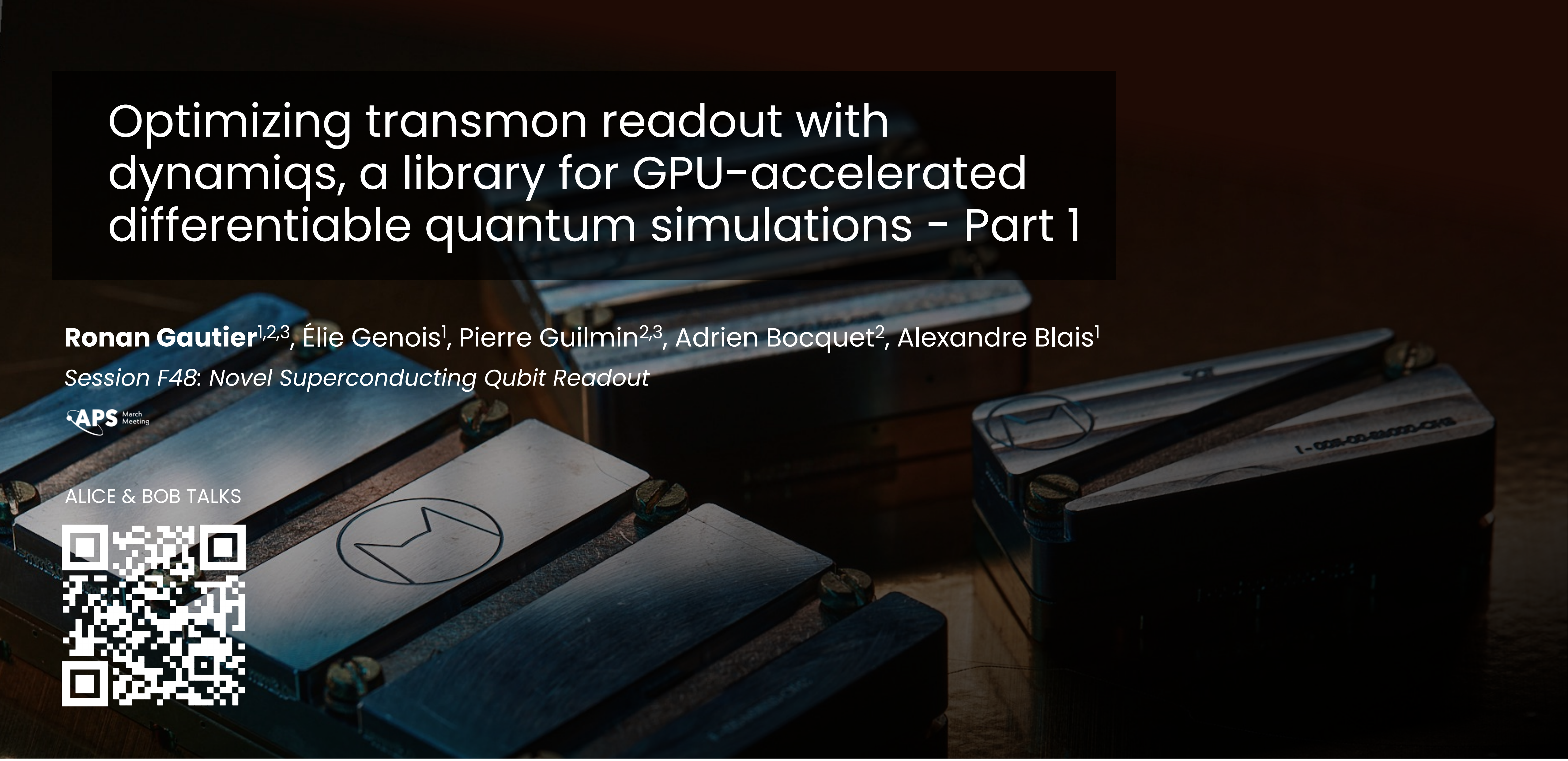

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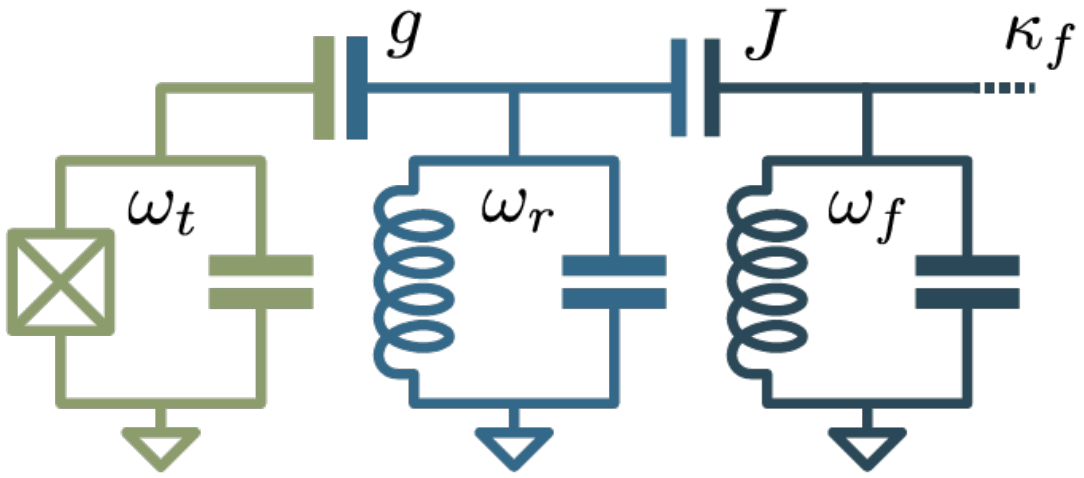
Dispersive readout

We want to optimize the dispersive readout of a transmon.

$$H = 4E_C n_t^2 - E_J \cos(\phi_t) + \omega_r a^\dagger a + \omega_f f^\dagger f + i g n_t (a^\dagger - a) + J(f^\dagger a + a^\dagger f)$$



- Full cosine model, <u>including</u> Purcell filter
- MW drive on Purcell filter and/or transmon

Difficult numerical problem

- ~400 parameters (1ns bins x 100ns x 2 drives)
- Hilbert space size ~ 8000 (5 x 40 x 40)
- GHz dynamics
- Open quantum system

Quantum optimal control

Gradient-free methods

- CRAB (Doria, PRL 2010)
- Nelder-Mead (Egger, PRL 2014)
- Model-free RL (Sivak, PRX 2022)

↳ Do not scale to many parameters

Gradient-based methods

- GRAPE (Boutin, PRA 2016)
- Krotov (Koch, JP:CM 2016)

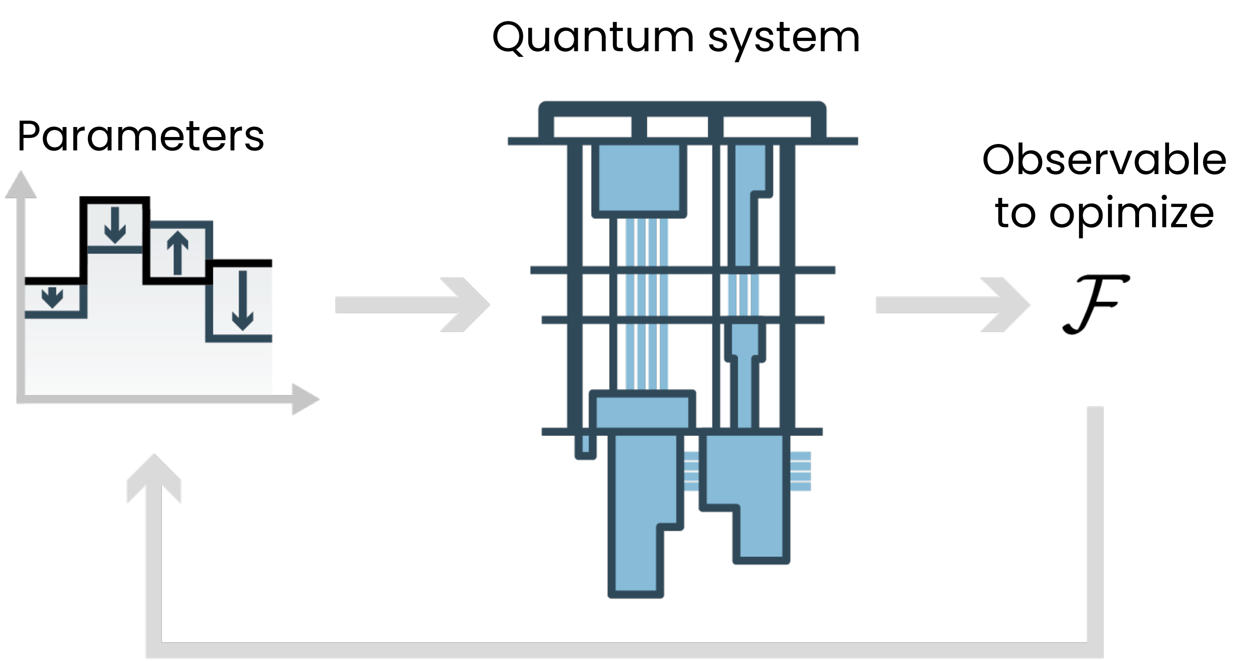
↳ Only state-to-state or gate optim.

- Automatic differentiation (Leung, PRA 2017)

↳ $O(N_T \times N^2)$ memory ➡ 4 Terabytes !

- Adjoint state method

↳ ✔ **Low memory + any closed or open system + any parametrized problem + fast**



Adjoint state method

- Parametrized master equation

$$\frac{d\rho}{dt} = \mathcal{L}\rho = -i[H,\rho] + \sum \mathcal{D}[L_k]\rho$$

$\hookrightarrow H = H(\theta)$ $\hookrightarrow L_k = L_k(\theta)$

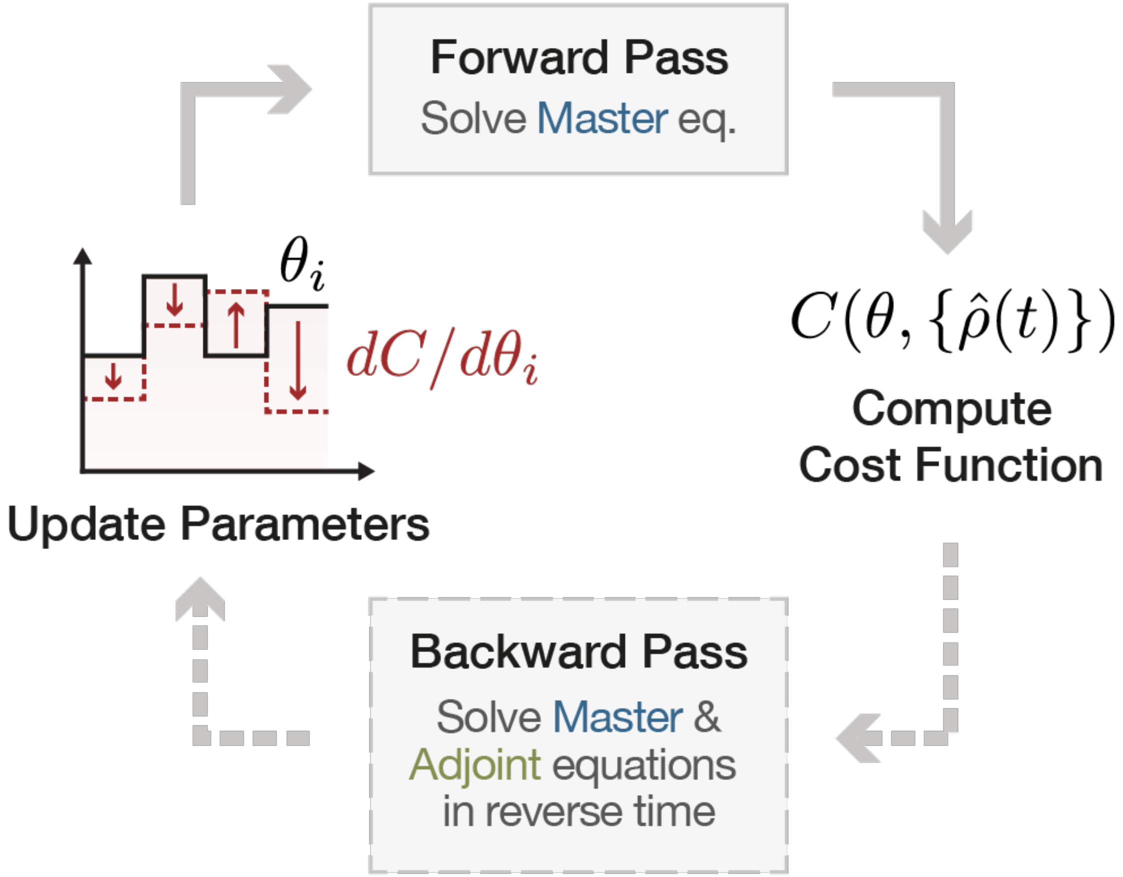
- Cost function $C = C(\theta, \rho(t_0), \ldots, \rho(t_n))$

- Adjoint state $\phi(t) = dC/d\rho(t)$

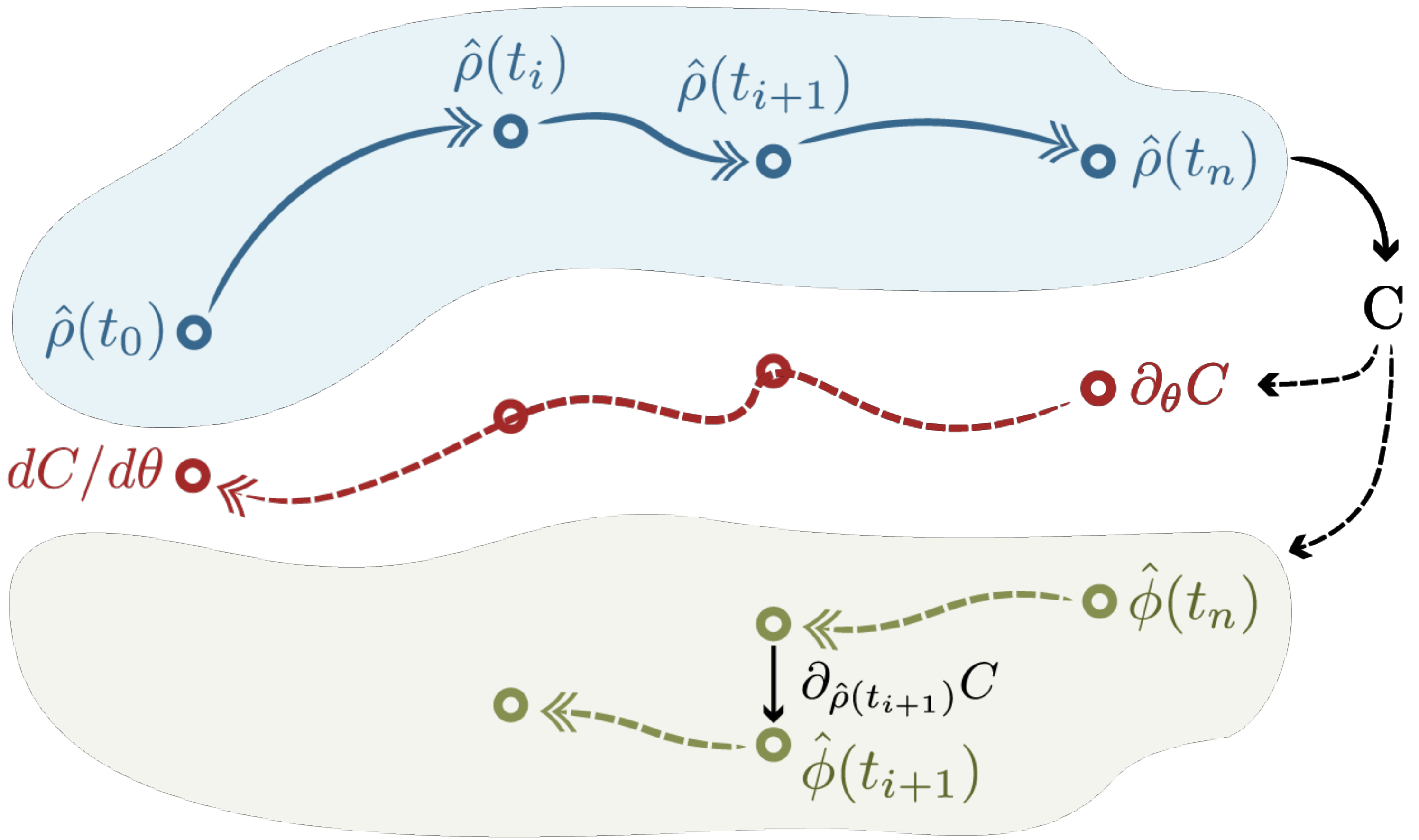
$$\frac{d\phi}{dt} = -\mathcal{L}^\dagger\phi = -i[H,\phi] - \sum \mathcal{D}^\dagger[L_k]\phi$$

- Explicit expression of gradient

$$\frac{dC}{d\theta} = \frac{\partial C}{\partial \theta} - \int_{t_0}^{t_n} \partial_\theta \mathrm{Tr}\left[\phi^\dagger(t)\mathcal{L}(t,\theta)\rho(t)\right] dt$$



Reverse-time backpropagation

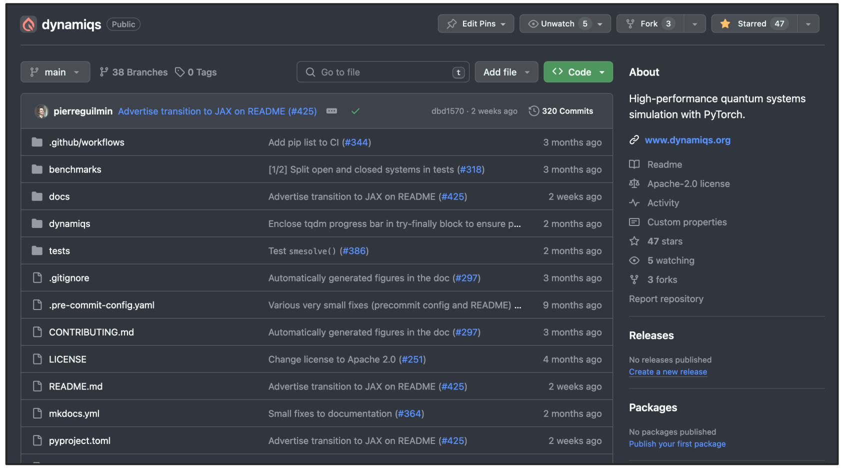


Memory: $\mathcal{O}(N^2)$ ➡ 488 MB

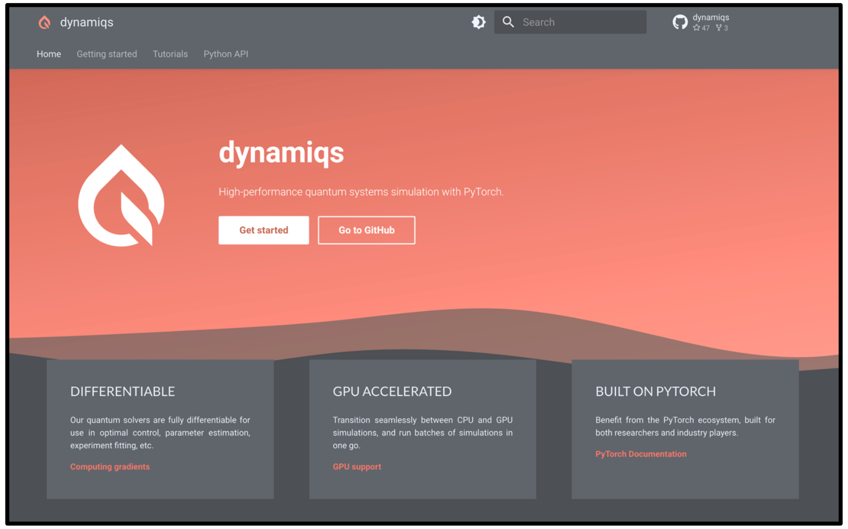
Optimal control with dynamiqs

- Open-source
- Closed, open and stochastic quantum systems
- End-to-end differentiable
- Works on GPUs → (very) fast simulations
- Batching
- QuTiP-like API
- …

github.com/dynamiqs



www.dynamiqs.org



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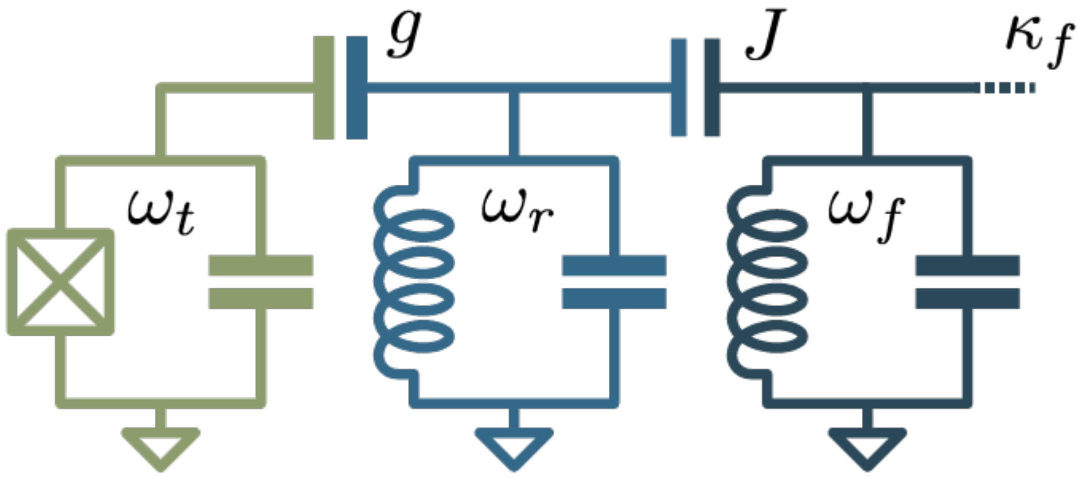


- Full cosine model, including Purcell filter
- MW drive on Purcell filter and/or transmon
- Optimisation with dynamiqs

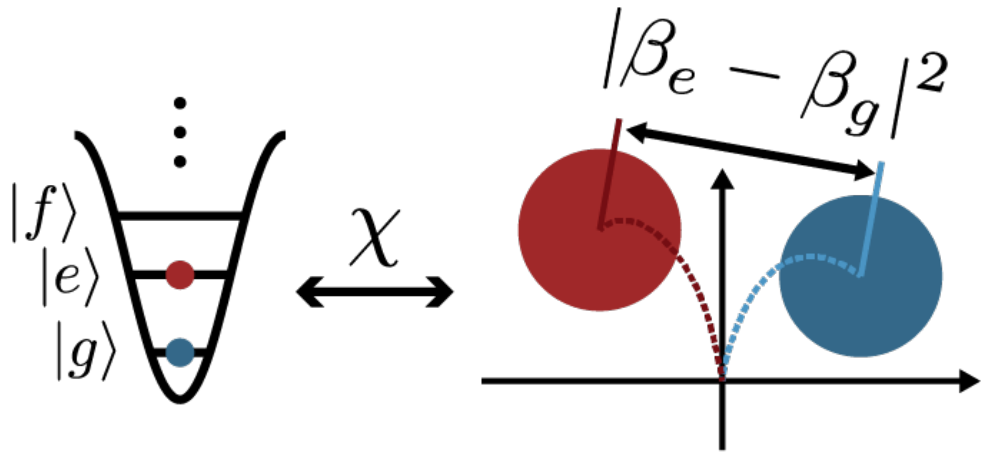
System parameters

$E_J/2\pi = 16\,\mathrm{GHz}$	$\omega_t/2\pi = 6\,\mathrm{GHz}$	$\kappa_p/2\pi = 30\,\mathrm{MHz}$	$g/2\pi = 150\,\mathrm{MHz}$
$E_c/2\pi = 315\,\mathrm{MHz}$	$\omega_r/2\pi = 7.2\,\mathrm{GHz}$	$\kappa_q/2\pi = 8\,\mathrm{KHz}$	$J/2\pi = 30\,\mathrm{MHz}$
$E_J/E_c \approx 51$	$\omega_p/2\pi = 7.21\,\mathrm{GHz}$	$\bar{n}_{\mathrm{crit}} = 16$	

Optimizing transmon readout

Signal-to-noise ratio (Bultink et al., 2017)

$$\mathrm{SNR} = \sqrt{2\eta\kappa_f \int_0^{\tau_m} dt\, |\beta_e - \beta_g|^2}$$

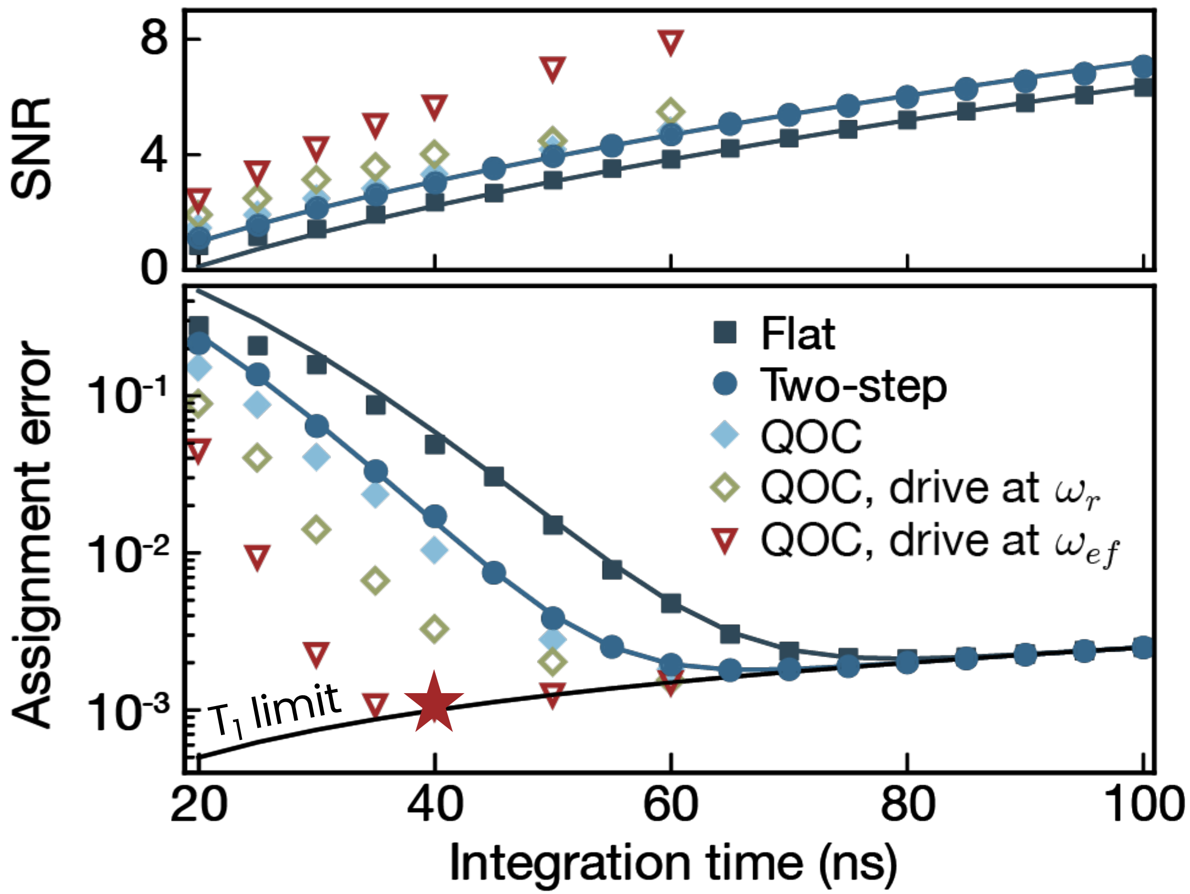


Optimizing transmon readout

Signal-to-noise ratio (Bultink et al., 2017)

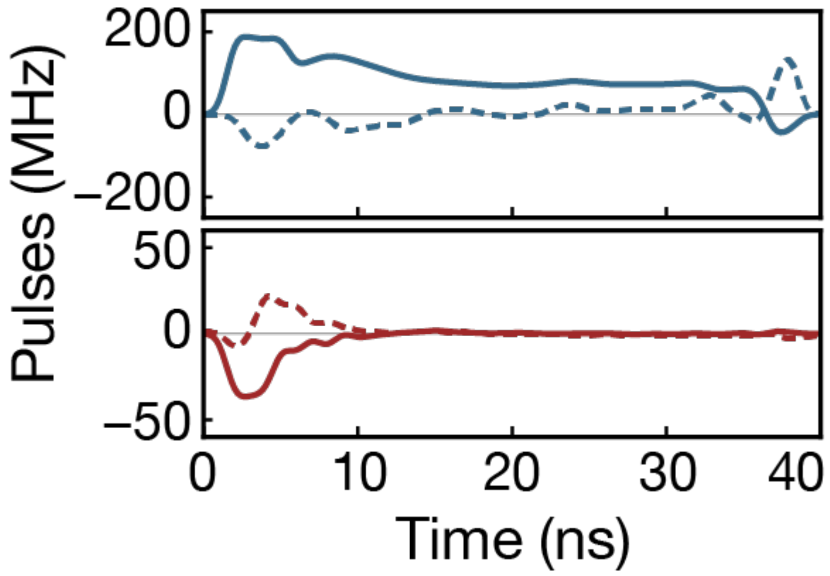
$$\mathrm{SNR} = \sqrt{2\eta\kappa_f \int_0^{\tau_m} dt\, |\beta_e - \beta_g|^2}$$

- 2 reference pulses
  - Flat pulse
  - Two-step pulse
- 3 optimized pulses
  - Drive filter
  - Drive filter + transmon @ w_r
  - Drive filter + transmon @ w_{ef}
- Optimize pulse envelopes
  + carrier frequencies
- Fair comparison: limit $n < n_{crit}$

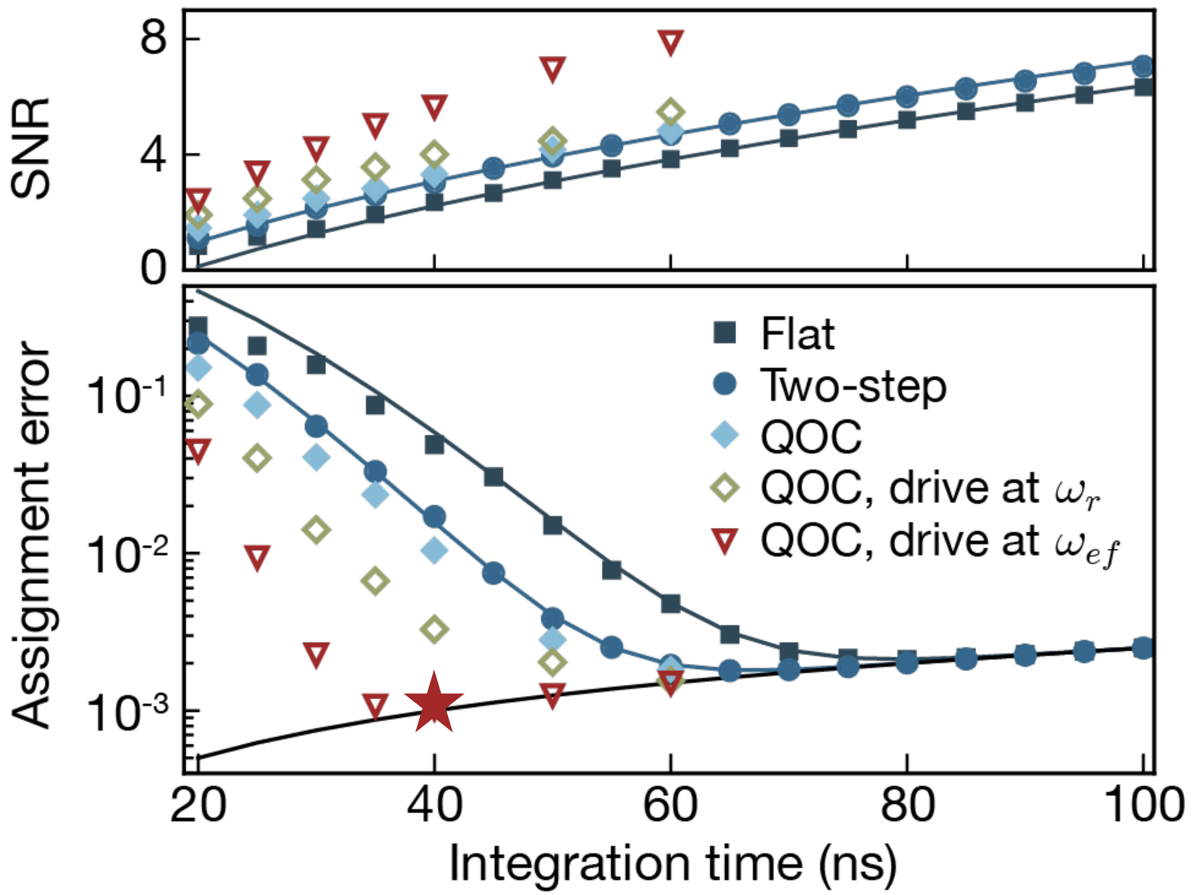


Shelving

QOC, drive @ w_{ef}



- Shelving (Elder, PRX 2020) & (Hann, PRA 2018)
  → use |f› state with larger coupling
- Filter envelope similar to two-step
- 10ns pi-pulse with DRAG & stark-shift
- **x2 improvement in readout time**



01. Optimal control w/ **adjoint state method**: low-memory, fast, generic

02. **Fast transmon readout** with additional drive on the transmon

03. **Realistic pulses** and known strategies found by optimizer

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Purcell filter trajectories

|g> and |e> trajectories in the Purcell filter → enhanced integrated distance